

Correlations

- ¾ When we want to consider if there is any relationship between two variables we can look for correlation or association
- ¾ A correlation is a measure of the linear relationship between variables. They could be
 - positively related
 - negatively related
 - not related at all
- ¾ Often a useful exploratory tool. But care needed; Spurious correlation -see Darrell Huffs book
- ¾ To compare two series we can describe their distribution about their mean. We would expect that if they are related they will vary from the mean in the same way for a particular observation. As we have seen the measure of the deviation from the mean of a sample is the variance:

$$\begin{aligned} \text{Variance} = s^2 &= \frac{\sum (X_j - \bar{X})^2}{N - 1} \\ &= \frac{\sum (X_j - \bar{X})(X_j - \bar{X})}{N - 1} \end{aligned}$$

- ¾ Note that s is the standard deviation (the square root of the variance)
- ¾ So one way of seeing if two variables is related is to see how they *covary*. Rather than squaring the difference we can multiply one difference by the other

$$\text{Covariance} = \text{cov}(X, Y) = \frac{\sum (X_j - \bar{X})(Y_j - \bar{Y})}{N - 1}$$

- ¾ A positive covariance will indicate that as one variable deviates from the mean in one direction so does the other.
- ¾ But this measure will depend upon the scale of the variables used -its just a value
- ¾ Need to standardise it so we get some idea of how strong the relation is and can compare such a relation between different variable pairs
- ¾ To do this we use the correlation coefficient r which looks at the covariance relative to their standard deviations

$$\begin{aligned} r &= \frac{\text{Cov}(X, Y)}{s_X s_Y} \\ &= \frac{\sum (X_j - \bar{X})(Y_j - \bar{Y})}{\sqrt{N - 1} s_X s_Y} \end{aligned}$$

- ¾ This is the Pearson product-moment correlation coefficient
- ¾ By standardising the covariance we have a value that has to lie between -1 and 1:
 - A correlation of +1 implies the variables are perfectly positively correlated
 - A correlation of -1 implies the variables are perfectly negatively correlated
 - A correlation of 0 implies the variables are not correlated
- ¾ NB this does not imply causality -association
- ¾ In SPSS can do correlations easily, but always worth doing a scatterplot first
- ¾ Problem with this measure is that as it looks at deviations from the mean it needs parametric data -need interval or ratio data
- ¾ If data are non parametric -when they are ordinal rather than cardinal or qualitative rather than quantitative- need to look at other methods provided by SPSS -rank correlation coefficients
 - Spearman's rho:
 - Kendall's tau
- ¾ Spearman's rho works by
 - first ranking the data and
 - then applying the Pearson equation for r

$$r = \frac{\text{Cov}(X, Y)}{s_X s_Y}$$

- ¾ Kendall's tau should be used when there is a small data set with a number of tied ranks